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Algebra II – Delta & Eta

Practicing Finding the Zeros of Quadratic  
Functions in Vertex Form  
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Name: Mr. Davis solutions

Solve each equation. Remember to use  $\pm$  to get all solutions.

$$\begin{aligned}32 &= 4(x-2)^2 & 8 &= (x-2)^2 \\ \pm\sqrt{8} &= \sqrt{(x-2)^2} \\ \pm 2\sqrt{2} &= x-2 \\ 2 \pm 2\sqrt{2} &= x \\ x &= 2+2\sqrt{2} & x &= 2-2\sqrt{2}\end{aligned}$$

$$\begin{aligned}9 &= (x+3)^2 & \pm\sqrt{9} &= \sqrt{(x+3)^2} \\ \pm 3 &= x+3 \\ -3 \pm 3 &= x \\ x &= -3+3 & x &= -3-3 \\ x &= 0 & x &= -6\end{aligned}$$

$$\begin{aligned}100 &= (7x-2)^2 - 25 \\ 125 &= (7x-2)^2 \\ \pm\sqrt{125} &= \sqrt{(7x-2)^2} \\ \pm 5\sqrt{5} &= 7x-2 \\ 2 \pm 5\sqrt{5} &= 7x \\ \frac{2 \pm 5\sqrt{5}}{7} &= x \\ x &= \frac{2+5\sqrt{5}}{7} & x &= \frac{2-5\sqrt{5}}{7}\end{aligned}$$

$$\begin{aligned}4 &= (x+10)^2 - 12 \\ 16 &= (x+10)^2 \\ \pm\sqrt{16} &= \sqrt{(x+10)^2} \\ \pm 4 &= x+10 \\ -10 \pm 4 &= x \\ x &= -10+4 & x &= -10-4 \\ x &= -6 & x &= -14\end{aligned}$$

Find the zeros of each quadratic function, which are the x-intercepts of the parabolas.

$f(x) = 2(x+1)^2 - 4$ $0 = 2(x+1)^2 - 4$ $4 = 2(x+1)^2$ $2 = (x+1)^2$ $\pm\sqrt{2} = \sqrt{(x+1)^2}$ $\pm\sqrt{2} = x+1$ $-1 \pm \sqrt{2} = x$ $x = -1 + \sqrt{2} \quad x = -1 - \sqrt{2}$	$f(x) = 3(x+1)^2 + 5$ $0 = 3(x+1)^2 + 5$ $-5 = 3(x+1)^2$ $-\frac{5}{3} = (x+1)^2$ <p>No real zeros. No x-intercepts; <math>(x+1)^2</math> cannot be negative.</p>	$f(x) = -5(x-4)^2 - 8$ $8 = -5(x-4)^2$ $-\frac{8}{5} = (x-4)^2$ <p>No real zeros No real solutions No x-intercepts <math>(x-4)^2</math> can't be negative</p>
$f(x) = x^2 + 3x$ $0 = x(x+3)$ $\downarrow \quad \downarrow$ $x=0 \quad x=-3$	$f(x) = (x-12)^2 + 8$ $0 = (x-12)^2 + 8$ $-8 = (x-12)^2$ <p>No real zeros No x-intercepts <math>(x-12)^2</math> cannot be negative</p>	$f(x) = 4(x+6)^2$ $0 = 4(x+6)^2$ $0 = (x+6)^2$ $\pm\sqrt{0} = \sqrt{(x+6)^2}$ $0 = x+6$ $x = -6$